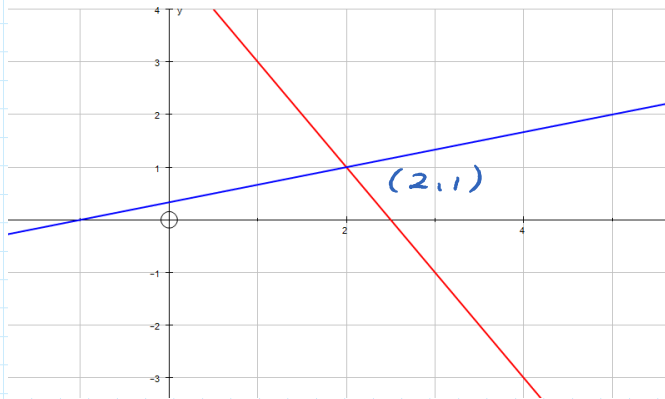


Solve

$$\begin{aligned} 2x + y &= 5 \\ x - 3y &= -1 \end{aligned}$$

$$\begin{array}{l} \times 3 \\ \times 1 \end{array}$$

$$\begin{array}{r} 6x + 3y = 15 \\ x - 3y = -1 \\ \hline 7x = 14 \\ x = 2 \\ y = 1 \end{array} \quad (2, 1)$$

Type 2: 3×3 Sim Eq

Solve

$$\begin{aligned} x + y + z &= -19 & \text{--- (i)} \\ 2x + 3y + z &= 16 & \text{--- (ii)} \\ 3x - 4y + 2z &= 1 & \text{--- (iii)} \end{aligned}$$

Elim z from (i) & (ii)

$$\begin{array}{r} -x + y + z = -19 \\ 2x + 3y + z = 16 \\ \hline x + 2y = -3 \end{array} \quad \text{--- (iv)}$$

Elim z from (ii) and (iii)

$$\begin{array}{r} 4x + 6y + 2z = 32 \\ -3x + 4y + 2z = 1 \\ \hline x + 10y = 31 \end{array} \quad \text{--- (v)}$$

Elim x from (iv) and (v)

$$\begin{array}{r} -x + 2y = -3 \\ x + 10y = 31 \\ \hline 8y = 28 \\ y = \frac{28}{8} = \frac{7}{2} \end{array}$$

Type 3: Substitution.

Solve $x + y = 3$ and $x^2 + y^2 = 5$

$$x^2 + y^2 = 5$$

$$x + y = \sqrt{5}$$

$$4 + 9 = 13$$

$$2 + 3 = \sqrt{13}$$

$$\sqrt{a} + \sqrt{b} \neq \sqrt{a+b}$$

$$\begin{array}{r} x + y = 3 \\ x^2 + y^2 = 5 \\ \hline x^2 + 2xy + y^2 = 9 \end{array}$$

$$\begin{array}{r} x + y = 3 \\ y = 3 - x \end{array}$$

$$x^2 + y^2 = 5$$

$$x^2 + (3-x)^2 = 5$$

$$x^2 + 9 - 6x + x^2 - 5 = 0$$

$$2x^2 - 6x + 4 = 0$$

$$x^2 - 3x + 2 = 0$$

$$(x-1)(x-2) = 0$$

$$x = 1 \quad x = 2$$

$$y = 3 - x$$

$$x = 1$$

$$y = 2$$

$$(1, 2)$$

$$x = 2$$

$$y = 1$$

$$(2, 1)$$

Solve $x + 2y = 5$ and

$$x^2 + y^2 = 10$$

$$2y = 5 - x$$

$$x + 2y = 5$$

$$y = \frac{5-x}{2}$$

$$x = 5 - 2y$$

$$(5 - 2y)^2 + y^2 = 10$$

$$(5-2y)^2 + y^2 = 10$$

$$25 - 20y + 4y^2 + y^2 = 10$$

$$5y^2 - 20y + 15 = 0$$

$$y^2 - 4y + 3 = 0$$

$$(y-1)(y-3) = 0$$

$$y-1=0$$

$$y-3=0$$

$$y=1$$

$$y=3$$

$$x = 5 - 2y$$

$$y=1 \Rightarrow x = 5 - 2(1) = 5 - 2 = 3$$

$$y=3 \Rightarrow x = 5 - 2(3) = 5 - 6 = -1$$

Solve $2x + 3y = 5$ and

$$x^2 + y^2 = 2.$$

$$2x + 3y = 5$$

$$2x + 3y = 5$$

$$3y = 5 - 2x$$

$$y = \frac{5-2x}{3}$$

$$x^2 + \left(\frac{5-2x}{3}\right)^2 = 2$$

$$x^2 + \frac{25 - 20x + 4x^2}{9} = 2$$

$$9x^2 + 25 - 20x + 4x^2 = 18$$

$$13x^2 - 20x + 7 = 0$$

$$\text{GUV } (13)(7)$$

$$\text{Add } -20$$

$$13x^2 - 13x - 7x + 7 = 0$$

$$13x(x-1) - 7(x-1) = 0$$

$$(x-1)(13x-7) = 0$$

$$x = 1 \quad x = \frac{7}{13}$$

$$y = \frac{5-2x}{3}$$

$$x = 1 \quad y = \frac{5-2}{3} = 1$$

$$x = \frac{7}{13} \quad y = \frac{5-2\left(\frac{7}{13}\right)}{3} = \frac{17}{13}$$

$$2x + 3y = 5$$

$$2x = 5 - 3y$$

$$x = \frac{5-3y}{2}$$

$$x^2 + y^2 = 2$$

$$\left(\frac{5-3y}{2}\right)^2 + y^2 = 2$$

$$\frac{25 - 30y + 9y^2}{4} + y^2 = 2$$

$$25 - 30y + 9y^2 + 4y^2 = 8$$

$$13y^2 - 30y + 17 = 0$$

Type 4: Become Simultaneous

$a(x+1) + b(x+3) = 5x + 9$ for a
x find a and b.

$$ax + a + bx + 3b = 5x + 9$$

$$ax + bx = 5x$$

$$-a + b = -5$$

$$a + 3b = 9$$

$$2b = 4$$

$$b = 2$$

$$a = 3$$

Write in form $(x+a)^2 + b$ and
solve $x^2 - 6x - 11 = 0$

$$x^2 - 6x - 11 = 0$$

$$x^2 - 6x + 9 - 11 - 9 = 0$$

$$(x-3)^2 - 20 = 0$$

$$(x-3)^2 = 20$$

$$x-3 = \pm\sqrt{20}$$

$$x = 3 \pm \sqrt{20}$$

$y = 5 - 8x - x^2$ find maximum

point.

$$\begin{aligned}y &= 5 - 8x - x^2 \\-y &= x^2 + 8x - 5 \\-y &= x^2 + 8x + 16 - 5 - 16 \\-y &= (x + 4)^2 - 21 \\y &= 21 - (x + 4)^2 \\ \text{Maximum} & \quad (-4, 21)\end{aligned}$$

Solve $(3x-1)^2 - 7(3x-1) - 8 = 0$

$$t = 3x - 1$$

$$t^2 - 7t - 8 = 0$$

$$(t - 8)(t + 1) = 0$$

$$t = 8$$

$$t = -1$$

$$3x - 1 = 8$$

$$3x - 1 = -1$$

$$3x = 9$$

$$3x = 0$$

$$x = 3$$

$$x = 0$$

Solve $x + y = 7$ and $x^2 + y^2 = 25$

$$x + y = 7$$

$$y = 7 - x$$

$$x^2 + (7 - x)^2 = 25$$

$$x^2 + 49 - 14x + x^2 - 25 = 0$$

$$2x^2 - 14x + 24 = 0$$

$$x^2 - 7x + 12 = 0$$

$$(x - 3)(x - 4) = 0$$

$$x = 3 \quad x = 4$$

$$y = 7 - x$$

$$y = 4 \quad y = 3$$

Solve $x - 3y = -1$ and $x^2 + y^2 = 5$

$$x - 3y = -1$$

$$x = 3y - 1$$

$$x^2 + y^2 = 5$$

$$(3y - 1)^2 + y^2 - 5 = 0$$

$$9y^2 - 6y + 1 + y^2 - 5 = 0$$

$$10y^2 - 6y - 4 = 0$$

$$5y^2 - 3y - 2 = 0$$

$$5y^2 - 5y + 2y - 2 = 0$$

$$5y(y-1) + 2(y-1) = 0$$

$$(y-1)(5y+2) = 0$$

$$y = 1 \quad y = -\frac{2}{5}$$

$$x = 3y - 1$$

$$x = 3 - 1 = 2$$

$$y = 1$$

$$y = -\frac{2}{5}$$

$$x = -\frac{6}{5} - \frac{1}{5} = -\frac{7}{5}$$