

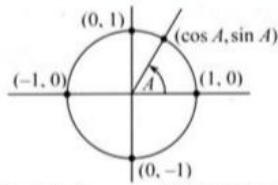
Must use the Index.

Triantánacht

Trigonometry

$$\tan A = \frac{\sin A}{\cos A} \quad \cot A = \frac{\cos A}{\sin A}$$

$$\sec A = \frac{1}{\cos A} \quad \operatorname{cosec} A = \frac{1}{\sin A}$$



$$\cos^2 A + \sin^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\cos(-A) = \cos A$$

$$\sin(-A) = -\sin A$$

$$\tan(-A) = -\tan A$$

Nóta: Bíonn $\tan A$ agus $\sec A$ gan sainiú nuair $\cos A = 0$.
Bíonn $\cot A$ agus $\operatorname{cosec} A$ gan sainiú nuair $\sin A = 0$.

Note: $\tan A$ and $\sec A$ are not defined when $\cos A = 0$.
 $\cot A$ and $\operatorname{cosec} A$ are not defined when $\sin A = 0$.

A (céimeanna)	0°	90°	180°	270°	30°	45°	60°	A (degrees)
A (raidiaín)	0	$\frac{\pi}{2}$	π	$\frac{3\pi}{2}$	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	A (radians)
$\cos A$	1	0	-1	0	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	$\cos A$
$\sin A$	0	1	0	-1	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	$\sin A$
$\tan A$	0	-	0	-	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	$\tan A$

1 rad. \approx 57.296°

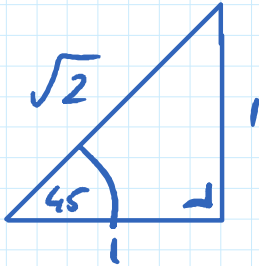
1° \approx 0.01745 rad.

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45°



$$1^2 + 1^2 = \sqrt{2}$$

$$\sin 45 = \frac{1}{\sqrt{2}}$$

$$\cos 45 = \frac{1}{\sqrt{2}}$$

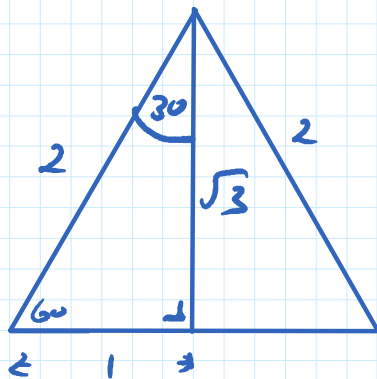
$$\tan 45 = 1$$

$$1^2 + x^2 = 2^2$$

$$x = \sqrt{3}$$

$$\sin 60 = \frac{\sqrt{3}}{2}$$

$$\cos 30 = \frac{\sqrt{3}}{2}$$



Equilateral
of side 2
Bisect the
angle which
will be
the perpendicular
bisector.

Unit Circle

2nd

Circle

90°

1st Quad

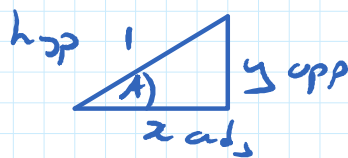
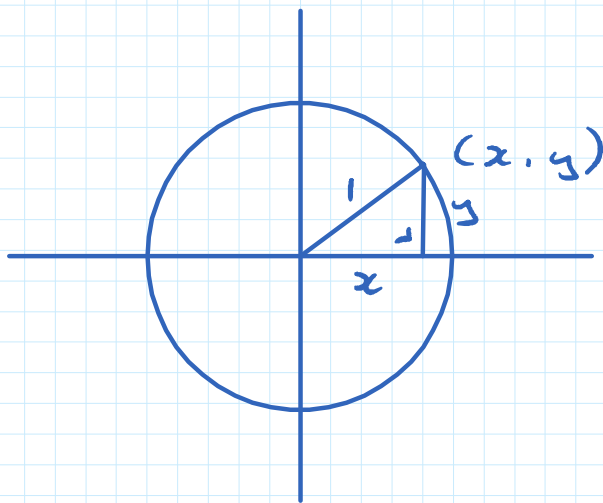
180° (-1, 0)

0°, 360°

3rd

270°

4th



$$\cos A = x$$

$$\sin A = y$$

$$(x, y) = (\cos A, \sin A)$$

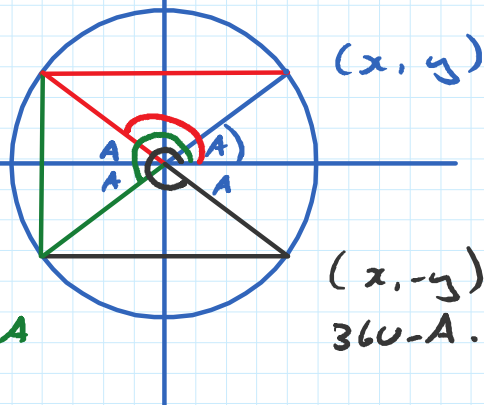
$$\tan A = \frac{y}{x} = \frac{\sin A}{\cos A}$$

cos -

sin +

tan -

(-x, y)
180-A



cos -

sin -

tan +

(-x, -y)
180+A

(x, -y)
360-A

cos +

sin +

tan +

cos +

sin -

tan -

Learn.
 Sin pos

Silly
 $\begin{array}{c} S + \\ C - \\ T - \end{array}$

$\begin{array}{c} S + \\ C + \\ T + \end{array}$

ALL ALL positive

Tan pos

Tom
 $\begin{array}{c} S - \\ C - \\ T + \end{array}$

$\begin{array}{c} S - \\ C + \\ T - \end{array}$

Cats Cos pos

$180 - \theta$

$\pi - \theta$

θ

$180 + \theta$

$\pi + \theta$

$360 - \theta$

$2\pi - \theta$

Solve

$\sin x = -\frac{\sqrt{3}}{2} \quad 0 \leq x \leq 360^\circ$

S	A
T	C
✓	✓

$\sin x = -\frac{\sqrt{3}}{2}$

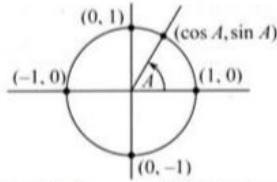
Sin is negative

Where is sin negative?
 3rd and 4th

Drop the sign

$\sin x = \frac{\sqrt{3}}{2}$ find x
 either with calc
 or tables.

$$\begin{aligned} \tan A &= \frac{\sin A}{\cos A} & \cot A &= \frac{\cos A}{\sin A} \\ \sec A &= \frac{1}{\cos A} & \operatorname{cosec} A &= \frac{1}{\sin A} \end{aligned}$$



$$\begin{aligned} \cos^2 A + \sin^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \cos(-A) &= \cos A \\ \sin(-A) &= -\sin A \\ \tan(-A) &= -\tan A \end{aligned}$$

Nóta: Bíonn tan A agus sec A gan sainiú nuair $\cos A = 0$.
Bíonn cot A agus cosec A gan sainiú nuair $\sin A = 0$.

Note: tan A and sec A are not defined when $\cos A = 0$.
cot A and cosec A are not defined when $\sin A = 0$.

A (céimeanna)	0°	90°	180°	270°	30°	45°	60°	A (degrees)
A (raidian)	0	$\frac{\pi}{2}$	π	$\frac{3\pi}{2}$	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	A (radians)
cos A	1	0	-1	0	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	cos A
sin A	0	1	0	-1	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	sin A
tan A	0	-	0	-	$\frac{1}{\sqrt{3}}$	1	$\sqrt{3}$	tan A

1 rad. $\approx 57.296^\circ$

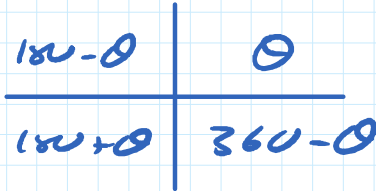
$1^\circ \approx 0.01745$ rad.

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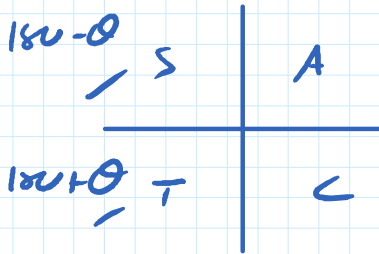
↳ to
Su line
arrows
to $\frac{\sqrt{3}}{2}$
↳ up $\Rightarrow \theta = 60^\circ$



Answers

$$\theta = 240^\circ \text{ or } 300^\circ$$

$$\cos \theta = -\frac{\sqrt{3}}{2}, \quad 0 \leq \theta \leq 360^\circ$$



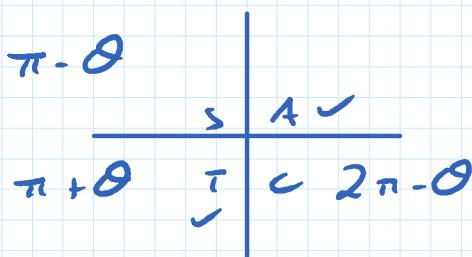
cos is negative
2nd + 3rd

$$\cos \theta = \frac{\sqrt{3}}{2} \Rightarrow 1^{\text{st}} \text{ quad answer}$$

$$\theta = 30^\circ \text{ (reference angle)}$$

$$\theta = 150^\circ \text{ or } 210^\circ$$

$$\tan A = \frac{1}{\sqrt{2}}, \quad 0 \leq A \leq 2\pi$$



Tan is positive
1st + 3rd

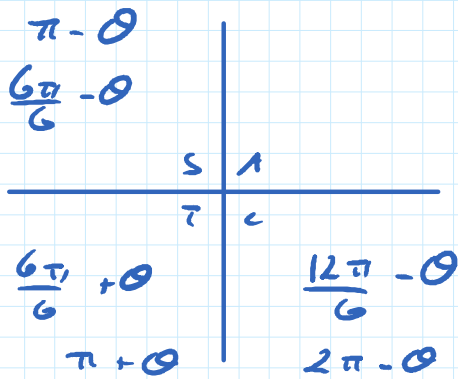
$$\tan A = \frac{1}{\sqrt{2}}$$

$$A = 0.615$$

$$A = 0.62 \quad \text{or} \quad 3.14 + 0.62$$

$$= 0.62 \text{ rads} \quad \text{or} \quad 3.76 \text{ radians.}$$

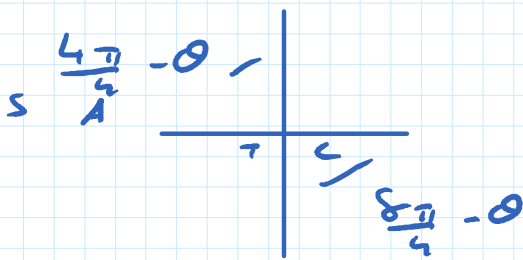
$$\sin \theta = \frac{1}{2} \quad \text{and} \quad 0 \leq \theta \leq 2\pi.$$



$$\sin \theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{6} \quad \text{or} \quad \frac{5\pi}{6}$$

$$\tan \theta = -1 \quad \text{and} \quad 0 \leq \theta \leq 2\pi.$$

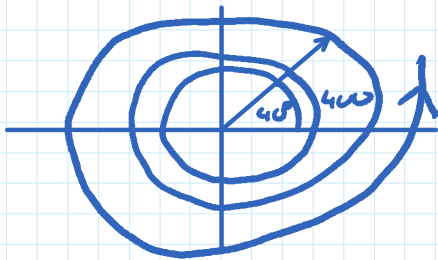


$$\tan \theta = 1$$

$$\theta = \frac{\pi}{4}$$

$$\theta = \frac{3\pi}{4} \quad \text{or} \quad \frac{7\pi}{4}$$

Revolutions.



$$400 = 400^\circ = 760$$

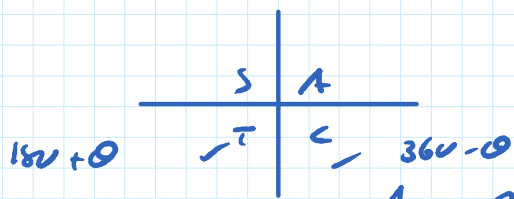
$$= 40 + 360n$$

$$n = 0 \Rightarrow \text{no full revolution}$$

$$n = 1 \Rightarrow 1 \text{ revolution}$$

$$n = 2 \Rightarrow 2 \text{ revolutions.}$$

$\sin A = -\frac{\sqrt{3}}{2}$ find A in degrees



$$\sin A = \frac{\sqrt{3}}{2}$$

$$A = 60^\circ$$

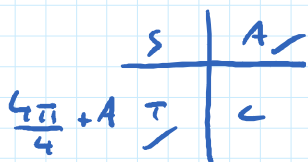
$$A = 240 + 360n$$

$$A = 300 + 360n$$

where $n \in \mathbb{N} \Rightarrow$ number of rotations.

These are called the general solutions.

$\tan \theta = 1$ find θ in radians.



$$\tan \theta = 1$$

$$\theta = \frac{\pi}{4} + 2n\pi$$

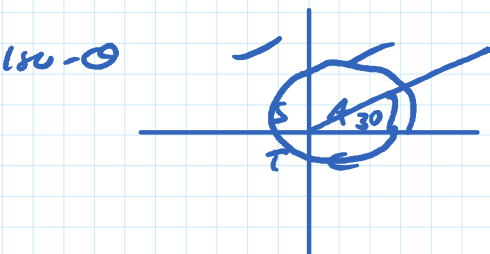
$$\theta = \frac{5\pi}{4} + 2n\pi$$

$A = 50$ find $\sin 3A$.

First $3A \Rightarrow 3(50) = 150$

Second $\sin 150 = \frac{1}{2}$.

$\sin 3A = \frac{1}{2}$ find $0 \leq A \leq 180^\circ$



$$0 \leq 3A \leq 540$$

$$3A = 30^\circ \quad 3A = 150$$

$$A = 10^\circ \quad A = 50^\circ$$

$$3A = 390 \quad 3A = 510$$

$$A = 130^\circ \quad A = 170^\circ$$

$$3A = 750$$

$$30^\circ = 390^\circ = 750^\circ = 1110^\circ$$

$$\cos 2A = -\frac{1}{2} \quad \text{find } 0 \leq A \leq 360^\circ.$$

$$\cos 2A = \frac{1}{2} \quad 0 \leq 2A \leq 720$$

$$2A = 60^\circ$$

150-0	✓
5	A
π	✓
150+0	✓

$$2A = 120 \text{ or } 240 \text{ or } 480 \text{ or } 600$$

$$A = 60 \text{ or } 120 \text{ or } 240 \text{ or } 300$$

$$2A = \cancel{840}$$

Rubrik.

$$A = 30$$

$$180 - 30$$

$$180 + 30$$

$$\tan 2A = -\sqrt{3}$$

3π/3 - 0	✓
5	A
π	✓
6π/3 - 0	✓

$$0 \leq A \leq \pi$$

$$0 \leq 2A \leq 2\pi$$

$$\tan 2A = \sqrt{3}$$

$$2A = \frac{\pi}{3}$$

$$2A = \frac{2\pi}{3} \quad \text{or} \quad \frac{5\pi}{3} \quad \text{or} \quad \cancel{\frac{8\pi}{3}}$$

$$A = \frac{\pi}{3} \quad \text{or} \quad \frac{5}{6}\pi$$

$$\frac{2\pi}{3} + \frac{6\pi}{3}$$