

Rates of Change

Distance (displacement) is a function of time.

$$\text{Distance} = s = f(t) = \text{m}$$

$$\text{Speed} = \frac{ds}{dt} = f'(t) = \text{m/s}$$

$$\text{Acceleration} = \frac{d^2s}{dt^2} = f''(t) = \text{m/s}^2$$

$$\text{Initial} \Rightarrow t = 0$$

$$\text{At rest} \Rightarrow \frac{ds}{dt} = 0$$

$$s = t^3 + 6t^2 + 5t + 7 \quad \text{Find}$$

(i) Initial distance

(ii) speed after 2 secs

(iii) acceleration after 4 seconds.

$$(i) \quad t = 0 \quad s = 7 \text{m}$$

$$(ii) \quad s = t^3 + 6t^2 + 5t + 7$$

$$\frac{ds}{dt} = 3t^2 + 12t + 5 \quad t = 2$$

$$\frac{ds}{dt} = 41 \text{ m/s}$$

$$(iii) \quad \frac{d^2s}{dt^2} = 6t + 12 \quad t=4$$
$$6(4) + 12 = 36 \text{ m/s}$$

Distance travelled after brakes are applied is given by $s = 18t - t^2$.
Find distance while at rest.

$$s = 18t - t^2$$
$$\frac{ds}{dt} = 18 - 2t = 0$$
$$t = 9 \text{ sec.}$$

$$s = 18(9) - 9^2$$
$$= 81 \text{ m}$$